

Solving Systems of Equations by Substitution

Name: _____ Date: _____

Solve each system by Substitution. Write the solution in the blank.

(-1, -2) 1.

$$\begin{aligned} y &= 2x \\ 2x + 3y &= -8 \end{aligned}$$

$$2x + 3(2x) = -8$$

$$2x + 6x = -8$$

$$8x = -8$$

$$x = -1$$

$$y = -2$$

(2, 9) 2.

$$\begin{aligned} y &= x + 7 \\ 2x + 3y &= 31 \end{aligned}$$

$$2x + 3(x + 7) = 31$$

$$2x + 3x + 21 = 31$$

$$5x = 10$$

$$x = 2 \quad y = 9$$

(-28, -7) 3.

$$\begin{aligned} x &= 4y \\ 3x - 10y &= -14 \end{aligned}$$

$$3(4y) - 10y = -14$$

$$12y - 10y = -14$$

$$2y = -14$$

$$y = -7$$

$$x = -28$$

(-1, 5) 4.

$$\begin{aligned} x &= -y + 4 \\ 4x + y &= 1 \end{aligned}$$

$$4(-y + 4) + y = 1$$

$$-4y + 16 + y = 1$$

$$-3y = -15$$

$$y = 5 \quad x = -1$$

(5, 15) 5.

$$\begin{aligned} x &= 2y - 25 \\ 3x - y &= 0 \end{aligned}$$

$$3(2y - 25) - y = 0$$

$$6y - 75 - y = 0$$

$$5y = 75$$

$$y = 15$$

$$x = 5$$

(-1, 3) 6.

$$\begin{aligned} 7x + 4y &= 5 \\ x &= 6y - 19 \end{aligned}$$

$$7(6y - 19) + 4y = 5$$

$$42y - 133 + 4y = 5$$

$$46y - 133 = 5$$

$$46y = 138$$

$$y = 3$$

$$x = -1$$

Solving Systems of Equations by Substitution

Solve each system by substitution.

$$1) \begin{cases} y = 6x - 11 \\ -2x - 3y = -7 \end{cases}$$

$$(2, 1)$$

$$-2x - 3(6x - 11) = -7 \quad -20x = -40$$

$$-2x - 18x + 33 = -7 \quad x = 2$$

$$-20x + 33 = -7 \quad y = 1$$

$$3) \begin{cases} y = -3x + 5 \\ 5x - 4y = -3 \end{cases}$$

$$(1, 2)$$

$$5x - 4(-3x + 5) = -3$$

$$5x + 12x - 20 = -3$$

$$17x = 17 \quad x = 1 \quad y = 2$$

$$5) \begin{cases} y = -2 \\ 4x - 3y = 18 \end{cases}$$

$$(3, -2)$$

$$4x - 3(-2) = 18$$

$$4x + 6 = 18$$

$$4x = 12 \quad x = 3$$

$$7) \begin{cases} -4x + y = 6 \\ -5x - y = 21 \end{cases}$$

$$(-3, -6)$$

$$y = 6 + 4x$$

$$-5x - (6 + 4x) = 21$$

$$-5x - 6 - 4x = 21$$

$$-9x = 27 \quad x = -3 \quad y = -6$$

$$9) \begin{cases} -5x + y = -2 \\ -3x + 6y = -12 \end{cases}$$

$$(0, -2)$$

$$y = -2 + 5x$$

$$-3x + 6(-2 + 5x) = -12$$

$$-3x - 12 + 30x = -12$$

$$-27x = 0 \quad x = 0$$

$$y = -2$$

$$2) \begin{cases} 2x - 3y = -1 \\ y = x - 1 \end{cases}$$

$$(4, 3)$$

$$2x - 3(x - 1) = -1$$

$$2x - 3x + 3 = -1$$

$$-x = -4 \quad x = 4 \quad y = 3$$

$$4) \begin{cases} -3x - 3y = 3 \\ y = -5x - 17 \end{cases}$$

$$(-4, 3)$$

$$-3x - 3(-5x - 17) = 3$$

$$12x = -48$$

$$-3x + 15x + 51 = 3$$

$$x = -4$$

$$12x + 51 = 3$$

$$6) \begin{cases} y = 5x - 7 \\ -3x - 2y = -12 \end{cases}$$

$$(2, 3)$$

$$y = 3$$

$$-3x - 2(5x - 7) = -12$$

$$-13x = -26$$

$$-3x - 10x + 14 = -12$$

$$x = 2$$

$$-13x + 14 = -12$$

$$y = 3$$

$$8) \begin{cases} -7x - 2y = -13 \\ x - 2y = 11 \end{cases}$$

$$(3, -4)$$

$$x = 11 + 2y$$

$$-7(11 + 2y) - 2y = -13$$

$$-77 - 14y - 2y = -13$$

$$-16y = 64$$

$$y = -4 \quad x = 3$$

$$10) \begin{cases} -5x + y = -3 \\ 3x - 8y = 24 \end{cases}$$

$$y = -3 + 5x$$

$$(0, -3)$$

$$3x - 8(-3 + 5x) = 24$$

$$3x + 24 - 40x = 24$$

$$36$$

$$-37x = 0$$

$$x = 0 \quad y = -3$$

$$11) \begin{cases} x+3y=1 \\ -3x-3y=-15 \end{cases}$$

$$(7, -2)$$

$$x = 1 - 3y$$

$$-3(1-3y) - 3y = -15$$

$$-3 + 9y - 3y = -15$$

$$-3 + 6y = -15 \quad 6y = -12 \quad y = -2$$

$$13) \begin{cases} -3x+3y=4 \\ -x+y=3 \end{cases}$$

$$y = 3 - x$$

$$-3x + 3(3-x) = 4$$

$$-3x + 9 + 3x = 4 \quad \text{parallel lines}$$

$$9 = 4 \leftarrow \text{no solution}$$

$$15) \begin{cases} 6x+6y=-6 \\ 5x+y=-13 \end{cases}$$

$$(-3, 2)$$

$$y = -13 - 5x$$

$$6x + 6(-13 - 5x) = -6$$

$$6x - 78 - 30x = -6$$

$$-24x = 72 \quad x = -3 \quad y = 2$$

$$17) \begin{cases} -3x-4y=2 \\ 3x+3y=-3 \end{cases}$$

$$(-2, 1)$$

$$3y = -3 - 3x$$

$$y = -1 - x$$

$$-3x - 4(-1-x) = 2$$

$$-3x + 4 + 4x = 2$$

$$x = -2 \quad y = 1$$

$$19) \begin{cases} -5x-8y=17 \\ 2x-7y=-17 \end{cases}$$

$$2x = -17 + 7y$$

$$x = -\frac{17}{2} + \frac{7}{2}y$$

$$-5\left(-\frac{17}{2} + \frac{7}{2}y\right) - 8y = 17$$

$$-5(-17 + 7y) - 16y = 34$$

$$85 - 35y - 16y = 34$$

$$12) \begin{cases} -3x-8y=20 \\ -5x+y=19 \end{cases}$$

$$(-4, 39)$$

$$y = 19 + 5x$$

$$-3x - 8(19 + 5x) = 20$$

$$-3x - 152 - 40x = 20$$

$$-43x = 172 \quad x = -4 \quad y = 39$$

$$14) \begin{cases} -3x+3y=3 \\ -5x+y=13 \end{cases}$$

$$(-3, -2)$$

$$y = 13 + 5x$$

$$-3x + 3(13 + 5x) = 3$$

$$-3x + 39 + 15x = 3$$

$$12x = -36 \quad x = -3 \quad y = -2$$

$$16) \begin{cases} 2x+y=20 \\ 6x-5y=12 \end{cases}$$

$$y = 20 - 2x$$

$$6x - 5(20 - 2x) = 12$$

$$(7, 6)$$

$$6x - 100 + 10x = 12$$

$$16x = 112$$

$$x = 7$$

$$y = 6$$

$$18) \begin{cases} -2x+6y=6 \\ -7x+8y=-5 \end{cases}$$

$$(3, 2)$$

$$-2x = 6 - 6y$$

$$x = -3 + 3y$$

$$x = 3$$

$$-7(-3 + 3y) + 8y = -5$$

$$21 - 21y + 8y = -5 \quad -13y = -26$$

$$y = 2$$

$$20) \begin{cases} -2x-y=-9 \\ 5x-2y=18 \end{cases}$$

$$-y = -9 + 2x$$

$$y = 9 - 2x$$

$$y = -2x + 9$$

$$(4, 1)$$

$$5x - 2(-2x + 9) = 18$$

$$5x + 4x - 18 = 18 \quad 37$$

$$x = 4 \quad y = 1$$

$$85 - 34 = 51 \quad y = 1 \quad x = 5$$